

# Gate-tunable strong spin-orbit interaction in two-dimensional tellurium probed by weak antilocalization

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Tellurium (Te) has attracted great research interest due to its unique crystal structure since the 1970s. However, the conduction band of Te is rarely studied experimentally because of the *p*-type accumulation layer at the surface of Te. By the atomic layer deposited dielectric doping technique, we are able to access the conduction-band transport properties of Te in a controlled fashion. In this paper, we report on a systematic study of the weak-anti-localization (WAL) effect in *n*-type two-dimensional (2D) Te films. We find that WAL agrees well with Iordanskii, Lyanda-Geller, and Pikus theory. The gate and temperature-dependent WAL reveal that the D'yakonov-Perel mechanism, dominant for spin relaxation and phase relaxation, is governed by electron-electron interaction. A large phase-coherence length near 600 nm at  $T = 1$  K is obtained together with gate-tunable spin-orbit interaction (SOI). Transition from weak-localization to WAL depending on gate bias is also observed. These results demonstrate that newly developed solution-based synthesized Te films provide a new controllable strong SOI 2D semiconductor with high potential for spintronic applications.

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Spin-orbit interaction (SOI) in two-dimensional (2D) materials brings many exotic phenomena to be explored. In transition-metal dichalcogenides, large SOI-induced band splitting in both conduction and valence bands gives rise to the valley Hall effect [1,2] and the unconventional quantum Hall effect [3,4]. Recently, band inversion caused by the spin-orbit coupling proximity effect [5] is observed in the graphene/WS<sub>2</sub> heterostructure [6]. SOI has been extensively studied in III-V semiconductors, such as InGaAs/InAlAs quantum wells for spintronic applications [7–9]. Chiral crystals with SOI are predicted to host Kramers-Weyl fermions and other topological quantum properties [10].

Weak-antilocalization (WAL) and weak localization (WL) caused by the interference of two time-reversal electron wave paths when electrons are scattered by impurities are used to probe SOI in conventional semiconductors [11] and now to be extended to 2D materials research, such as graphene [12,13], MoS<sub>2</sub> [14,15], black phosphorus [16–19], and others [20–23]. A correction to magnetoconductance due to the backscattered constructive or destructive interference between electrons is sensitive to the phase coherence and spin relaxation of electrons. WAL is also found in topologically nontrivial systems, such as topological insulators [24,25], Dirac [26], and Weyl [27] semimetals due to the significant Berry's phase.

Tellurium (Te) is a narrow band-gap (0.35-eV) semiconductor with a hexagonal crystal structure formed by van der Waals interaction between each one-dimensional helical atom chain. Covalently bonded atoms rotate around the *c* axis in a period of three atoms as shown in Fig. 1(a). The valence band

and conduction band are located in the corner of Brillouin zone *H* and *H'* points [Fig. 1(b)]. Theoretically, Te is predicted to undergo transformation into a topological insulator under strain [28] and a Weyl semimetal under pressure [29]. Te has a *p*-type accumulation layer at the surface [30], therefore, up to date, most of the experiments including thermoelectric properties [31], quantum Hall effect [32], and angle-resolved photoemission spectroscopy [33] were performed in *p*-type Te samples. The lack of inversion symmetry and the strong spin-orbit coupling of Te give rise to the camelbacklike structure in the valence band [32] and Rashba-like spin splitting bands with nontrivial radial spin texture in the conduction band [29,34]. The spin-split conduction bands cross at the *H* point and form a Weyl point protected by the threefold screw symmetry of the helical crystal [28]. The spin-orbit interaction and its mechanism in *n*-type Te is explored here.

In this paper, we perform magnetotransport measurements of 2D *n*-type Te at cryogenic temperatures. WAL is observed at low magnetic fields less than 0.2 T. Temperature and gate-dependent WAL are systematically measured and analyzed. The spin-relaxation and phase-relaxation mechanisms are studied, showing the high quality of the 2D Te film and the existing strong SOI in this material.

The inset of Fig. 1(c) is an optical image of a Te device with a Hall-bar structure for magnetotransport studies. Source and drain electrodes were made along the long edge of the flake which coincides with the direction of the atomic chains [35]. Hall bars are used to measure the longitudinal and transverse resistances with the backgate to tune the film electron density. The sketch of a typical *n*-type field-effect device is shown in Fig. 1(d). The 20-nm Al<sub>2</sub>O<sub>3</sub> is grown by atomic layer deposition at 200 °C to dope tellurium into *n* type [36,37]. A similar effect has also been observed in black phosphorus

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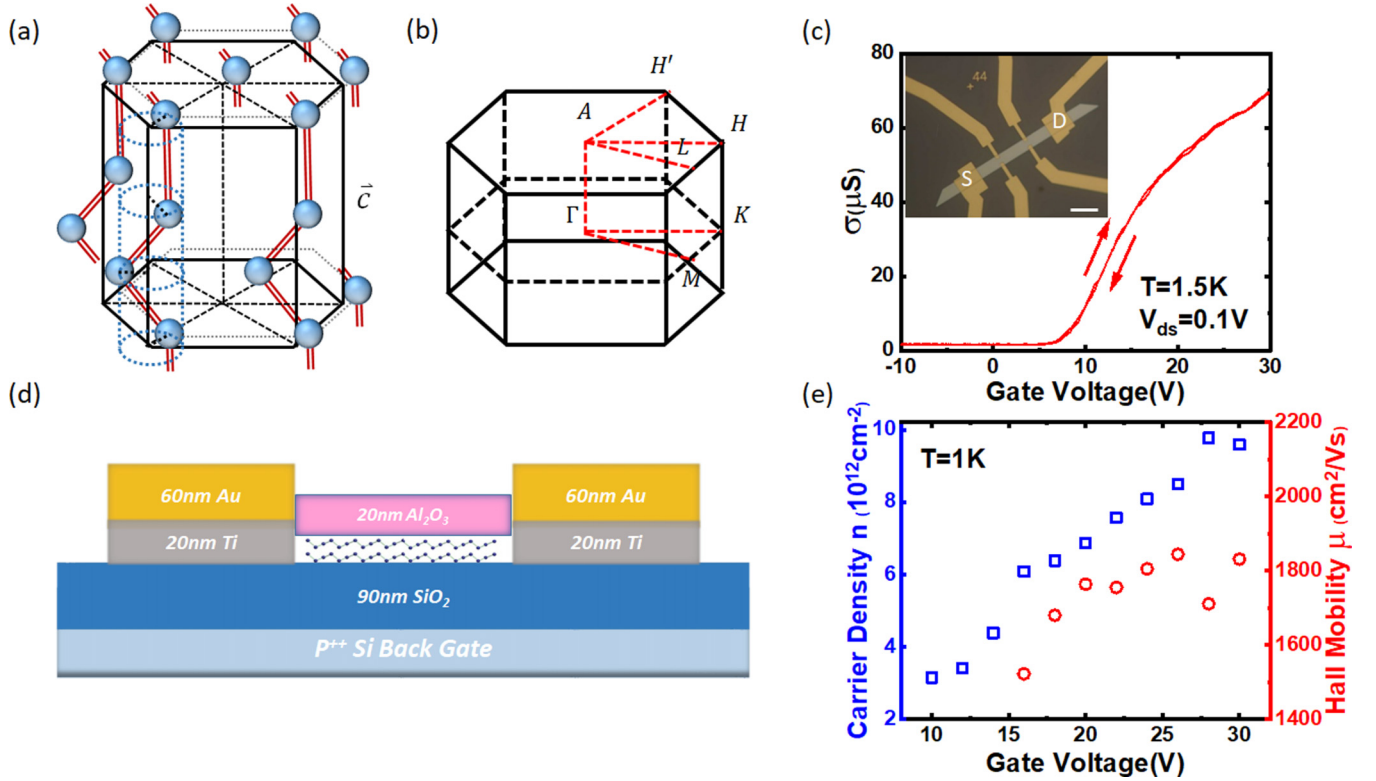


FIG. 1. (a) Crystal structure of Te. Te has one-dimensional helical atom chains along the  $\bar{c}$  direction and the hexagonal structure is formed by van der Waals interaction between each chain. (b) The first Brillouin zone of Te. The Te conduction-band minima are located in  $H$  and  $H'$  points. (c) Transfer curve of a  $n$ -type Te field-effect device with a Te film thickness of  $10\text{ nm}$  at  $1.5\text{ K}$ . The inset: An optical image of a Hall-bar device for transport measurement with helical atom chains ( $c$  axis) along the long edge of the flake. The scale bar is  $20\text{ }\mu\text{m}$ . (d) Device structure sketch of a  $n$ -type Te field-effect transistor. (e) Gate-dependent carrier density  $n$  (blue squares, left axis) and electron mobility  $\mu$  (red circles, right axis) extracted from the Hall measurement at  $1\text{ K}$ .

[38,39]. Tellurium flakes with thicknesses around  $10\text{ nm}$  are transferred onto a  $90\text{-nm SiO}_2/\text{Si}$  substrate, which served as a backgate for the transistor, and  $20\text{-nm Ti}/60\text{-nm Au}$  are used for  $n$ -type contact. In order to prove the  $n$ -type doping effect, a transfer curve of a Te field-effect device is measured [Fig. 1(c)] using a four-terminal method. By carrying out the Hall measurement, we can calculate the two-dimensional carrier density  $n$  and electron Hall mobility  $\mu$  under different gate biases [Fig. 1(e)] using  $n = \frac{1}{e}(\frac{dB}{dR_{xx}})$  and  $\mu = (\frac{L}{W})(\frac{1}{R_{xx}ne})$ , where  $L$  is the channel length,  $W$  is the channel width,  $R_{xx}$  is the longitudinal resistance, and  $R_{xy}$  is the Hall resistance. More than ten devices were fabricated and measured, all of which show similar and reproducible behaviors. All the results presented below are from one representative device. Another  $n$ -type Te WAL device is analyzed in the Supplemental Material [40]. WAL is also measured and analyzed in undoped intrinsic  $p$ -type 2D Te films with gate and temperature dependence as shown in the Supplemental Material [40].

Two different spin-relaxation mechanisms can be used to explain the formation of WAL: the D'yakonov-Perel (DP) and the Elliot-Yafet (EY) spin-relaxation mechanisms [41]. The EY spin-relaxation mechanism often exists in spin degenerated bands in which spin-up and spin-down states are entangled by SOI. When an elastic-scattering (momentum-scattering) process occurs, the electron spin may flip during the scattering. The DP spin relaxation is attributed to the

spin-precession process caused by an effective magnetic-field  $B_{\text{eff}}$  ( $B_{\text{eff}} \propto \vec{E} \times \vec{p}$  [42,43] where  $\vec{E}$  is the electric field and  $\vec{p}$  is the electron momentum) which is induced by Rashba [44] and/or Dresselhaus SOI [45]. The electron spin makes the precession along the effective magnetic-field direction during the elastic-scattering process. The scattering of an electron by impurities and phonons which changes the electron momentum  $\vec{p}$ , fluctuate the effective magnetic-field  $\vec{B}_{\text{eff}}$  and suppress the spin relaxation. Therefore, the spin-relaxation time  $\tau_{\text{so}}$  is proportional to the momentum-scattering time  $\tau_{\text{tr}}$  for the EY spin-relaxation mechanism and inversely proportional to  $\tau_{\text{tr}}$  for the DP mechanism [21,46]. Rashba SOI induced by the external electric field and Dresselhaus SOI induced by crystal electric field in inversion asymmetric materials contribute to band spin splitting even at zero external magnetic field.

WAL based on the EY spin-relaxation mechanism is described by the Hikami, Larkin, and Nagaoka (HLN) theory [47], meanwhile, the Iordanskii, Lyanda-Geller, and Pikus (ILP) [48] theory is based on the DP mechanism. Both theories are valid when the external magnetic-field  $B$  is smaller than the characteristic magnetic field for transport  $B_{\text{tr}}$  ( $B_{\text{tr}} = \hbar/4eD\tau_{\text{tr}}$  where  $D$  is the diffusion constant and  $\tau_{\text{tr}}$  is the momentum-scattering time).  $B_{\text{tr}}$  in  $n$ -type Te is determined to be  $0.2\text{ T}$  in the Supplemental Material [40]. All the results in this paper are from the fitting of data below  $0.2\text{ T}$ . Zero-field conductivity is calculated to be much larger than  $\frac{e^2}{h}$ , therefore,

the effect of small conductivity on weak localization [49] is not considered in this paper. Fittings of Te WAL experimental data with both theories are shown in Fig. 2 where the red line presents for ILP theory and the blue line presents for HLN theory in the Supplemental Material [40]. It is clear that the

ILP fitting provides better agreement with experimental data, indicating that the DP spin-relaxation mechanism is dominant in Te single-crystal films.

Magnetoconductance of WAL using ILP theory is expressed as shown below [41,46],

$$\sigma_{xx}(B) - \sigma_{xx}(0) = \frac{e^2}{2\pi^2\hbar} \left\{ \Psi\left(\frac{1}{2} + \frac{B_\varphi}{B} + \frac{B_{so}}{B}\right) - \ln \frac{B_\varphi + B_{so}}{B} + \frac{1}{2} \Psi\left(\frac{1}{2} + \frac{B_\varphi}{B} + \frac{2B_{so}}{B}\right) - \frac{1}{2} \ln \frac{B_\varphi + 2B_{so}}{B} \right. \\ \left. - \frac{1}{2} \Psi\left(\frac{1}{2} + \frac{B_\varphi}{B}\right) + \frac{1}{2} \ln \frac{B_\varphi}{B} \right\} \\ B_x = \frac{\hbar}{4eD\tau_x}, \quad L_x = \sqrt{D\tau_x}, \quad x = so, \varphi, \quad B_{so} = \frac{\hbar}{4eD} |\Omega_3|^2 \tau_{tr}, \quad (1)$$

where  $e$  is the elementary charge,  $\hbar$  is the reduced Planck constant,  $\psi$  is the function,  $D$  is the diffusion constant,  $\tau_\varphi$  is the phase-relaxation time,  $\tau_{so}$  is the spin-relaxation time,  $\Omega_3$  is the  $k$ -cubic-dependent spin-precession vector,  $L_{so}$  and  $L_\varphi$  are the spin-relaxation length and phase-coherence length, respectively.  $B_\varphi$  and  $B_{so}$  are the only two fitting parameters. From the ILP fitting in the Supplemental Material [40], we conclude that the  $k$ -linear SOI effect is much smaller than the  $k$ -cubic SOI effect in our Te sample which is different from III-V semiconductors because, according to Fig. S2 in the Supplemental Material [40], the fittings are good when the  $k$ -linear term is small. The intervalley scattering is also considered in the Supplemental Material [40].

In order to extract  $\tau_{so}$  from  $B_{so}$ , the diffusion constant  $D$  ( $D = v_F^2 \tau_{tr}/2$ , where  $v_F$  is the Fermi velocity) and the effective mass  $m^*$  are calculated from Hall measurement and temperature-dependent Shubnikov-de Haas oscillations in the Supplemental Material [40]. We are able to extract the effective mass of electrons  $m_e^* = 0.11m_0$ , where  $m_0$  is the bare electron mass (see Fig. S1 in the Supplemental Material [40]). This is consistent with the previous theoretical prediction [50]. The Te conduction-band minimum is at the  $H$  point of the Brillouin zone [Fig. 1(b)] which has twofold valley degeneracy and twofold spin degeneracy [29]. To better

understand the spin-relaxation mechanism in Te, the density dependence of WAL is measured and analyzed [Fig. 3(a)]. The relation between spin-relaxation time  $\tau_{so}$  and momentum-scattering rate  $\tau_{tr}^{-1}$  [40] is presented in Fig. 3(b). The red eye guideline indicates that  $\tau_{so}$  is inversely proportional to  $\tau_{tr}$ . This result together with the better fitting of experimental data with ILP theory unveils that DP spin-relaxation mechanism (spin precession) is dominant in  $n$ -type 2D Te films.

$B_\varphi(L_\varphi)$  and  $B_{so}(L_{so})$  are extracted from WAL curves [Figs. 3(c) and 3(d)]. The phase-coherence length  $L_\varphi$  reaches as high as 573 nm at  $V_{bg} = 30$  V which is larger than that of  $p$ -type Te [51] (Fig. S9c of the Supplemental Material [40]) and other 2D materials [14,15,20–22,43,51–54]. It is worth mentioning that the elastic-scattering length is extracted to be  $L_e$  (23–47 nm) which is one order of magnitude smaller than the phase-coherence length in all gate voltages. Thus, the electron transport in  $n$ -type Te at low temperatures is in the quantum diffusive regime. In addition, the decrease in spin-relaxation length  $L_{so}$  with the gate voltage can only be explained by the decrease in  $\tau_{so}$  (stronger SOI) at a higher gate voltage because  $D$  is increasing with gate voltage according to  $L_{so} = \sqrt{D\tau_{so}}$  and  $D = v_F^2 \tau_{tr}/2$ . This further confirms that spin splitting can be tuned by the gate in  $n$ -type Te. The gate-tunable SOI together with the long phase-coherence length gives 2D Te a new edge for spintronic applications over other 2D materials that either lack controllable SOI (such as graphene [12,13]) or suffer from short phase-coherence length. The phase-coherence length  $L_\varphi$  increases with back-gate-voltage  $V_{bg}$ , implying that electron-electron (e-e) scattering is the main phase-relaxation mechanism. We will further discuss the dephasing mechanism below, which plays an important role in the formation of WAL.

Both Rashba and Dresselhaus SOI have  $k$ -cubic-dependent spin-precession vector  $\Omega_3$  [44] and the strength are increasing with carrier density, thus, Fermi vector. However, the strength of the Rashba term is also controlled by the external electric field (induced by gate voltage). Here, the relation between  $\Omega_3$  and  $k_F^3$  (extracted from  $B_{so}$  and carrier density  $n$ ) are plotted in Fig. 4. Linear fitting of the data (red solid line) shows a change at  $V_{bg} = 16$  V ( $D = 0.69$  V/nm) which indicates that both Rashba and Dresselhaus SOIs exist in  $n$ -type Te and the Rashba effect occurs after the displacement field is larger than  $D = 0.69$  V/nm. We estimate the spin-splitting energy is approximately 2.6–8 meV from  $2\Delta = 2\hbar|\Omega_3|$  [44].

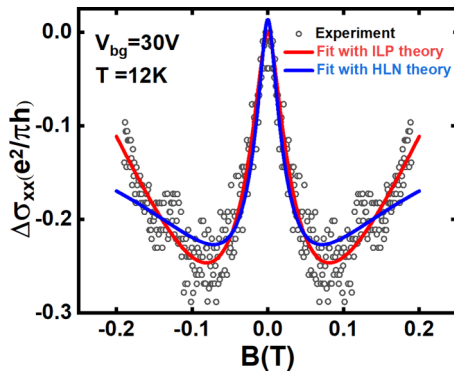


FIG. 2. Experimental WAL data (black circles) measured at  $T = 12$  K  $V_{bg} = 30$  V and fitting curves with different theories (red line for the ILP theory, blue line for the HLN theory). The IPL theory (red line) provides better agreement with experimental data. Zero-field conductivity is calculated ( $\sigma_{xx} = 228.8 e^2/\pi h$ ).

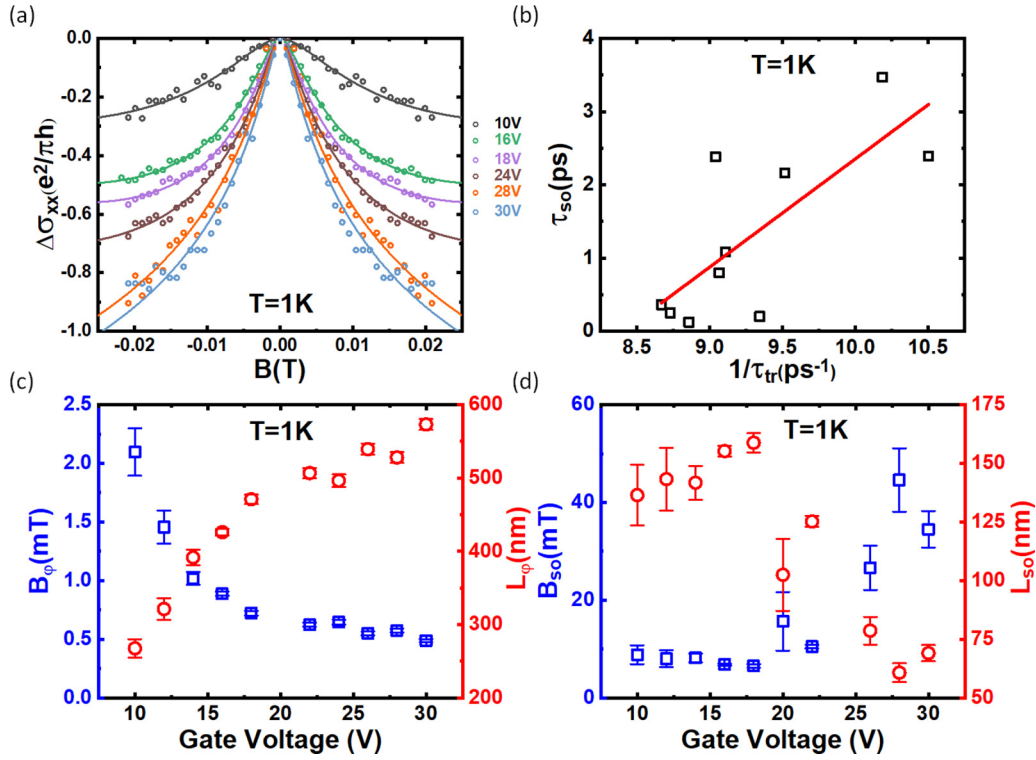


FIG. 3. Gate dependence of WAL. (a) Theoretical fits (solid lines) with ILP theory to experimental data (circles) measured at various backgate voltages. Zero-field conductivity is calculated ( $\sigma_{xx} = 64.1 - 227.9 e^2/\pi h$ ). (b) Spin-relaxation time  $\tau_{so}$  as a function of momentum-scattering rate  $\tau_{tr}^{-1}$  at  $T = 1$  K. The red solid line is the linear fit of data points. The positive correlation between  $\tau_{so}$  and  $\tau_{tr}^{-1}$  indicates the DP spin-relaxation mechanism is dominant in Te. (c) Gate-dependent  $B_\phi$  (blue squares, left axis) and phase-coherence length  $L_\phi$  (red circles, right axis) extracted from the WAL fitting at  $T = 1$  K. (d) Gate-dependent  $B_{so}$  (blue squares, left axis) and spin-relaxation length  $L_{so}$  (red circles, right axis) extracted from the WAL fitting at  $T = 1$  K.

In general, phase-coherence length is limited by inelastic electron-electron scattering and electron-phonon (e-ph) scattering [20]. For inelastic electron-electron scattering with small energy transfer, phase-coherence length  $L_\phi$  is expressed as [17]

$$L_\phi = \frac{\hbar^2 \sigma_{xx}}{\pi e^2} \left( m^* k_B T \ln \frac{\sigma_{xx} \hbar}{e^2} \right)^{-1/2}, \quad (2)$$

by the Altshuler-Aronov-Khmelnitsky (AAK) theory [55]. To further investigate the inelastic-scattering mechanism of Te,

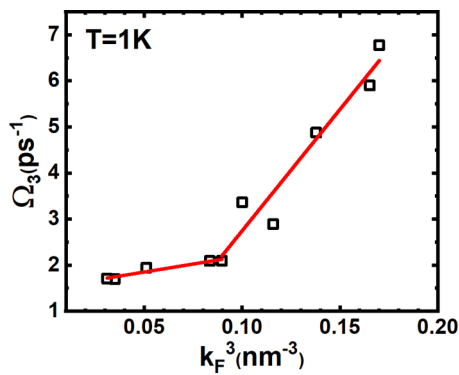


FIG. 4. The relation between  $k$ -cubic spin-precession vector  $\Omega_3$  and Fermi vector  $k_F^3$ . Two stages are shown in the plot (red solid lines): the change in the slope means that the Rashba effect is strong after  $V_{bg} = 16$  V ( $D = 0.69$  V/nm).

temperature-dependent WAL is also measured as shown in Fig. 5(a). When the temperature increases, WAL peaks attenuate because of the decrease in the phase-coherence length [Fig. 5(b)]. The temperature-dependent phase-coherence length  $L_\phi \propto T^{-\gamma}$  distinguishes different scattering mechanisms. For example,  $\gamma = 1$  is for e-ph interaction and  $\gamma = 0.5$  is for e-e interaction [20,22]. The Fig. 5(b) inset presents gate-dependent  $\gamma$  extracted from the power-law fitting of  $L_\phi$ . Measured values of  $\gamma$  are close to 0.5 in all gate ranges which is in good agreement with AAK theory described in Eq. (2). The slight deviation from 0.5 can be explained by the temperature dependence of  $\sigma_{xx}$ . By plotting experimentally extracted  $L_\phi$  as a function of conductance  $\sigma_{xx}$  [Fig. 5(c)], we can confirm that the near-linear dependence between gate voltage and phase-coherence length at fixed temperatures originates from electron-electron interaction. Therefore, we conclude that electron-electron interaction is the main phase-relaxation mechanism in Te within temperatures ranging from 1 to 18 K.

Interestingly, quantum interference effects, such as WL and WAL, are sensitive to the relative strength of spin relaxation and phase coherence as we discussed before. The system shows WAL when the phase-coherence length is larger than the spin-relaxation length and WL otherwise [43]. The gate-dependent transition from WAL to WL is observed at a higher temperature (18 K) [Fig. 5(d)]. According to the AAK theory [Eq. (2)], the phase-coherence length  $L_\phi$  is small in the region of high temperatures and low gate voltage (low longitudinal

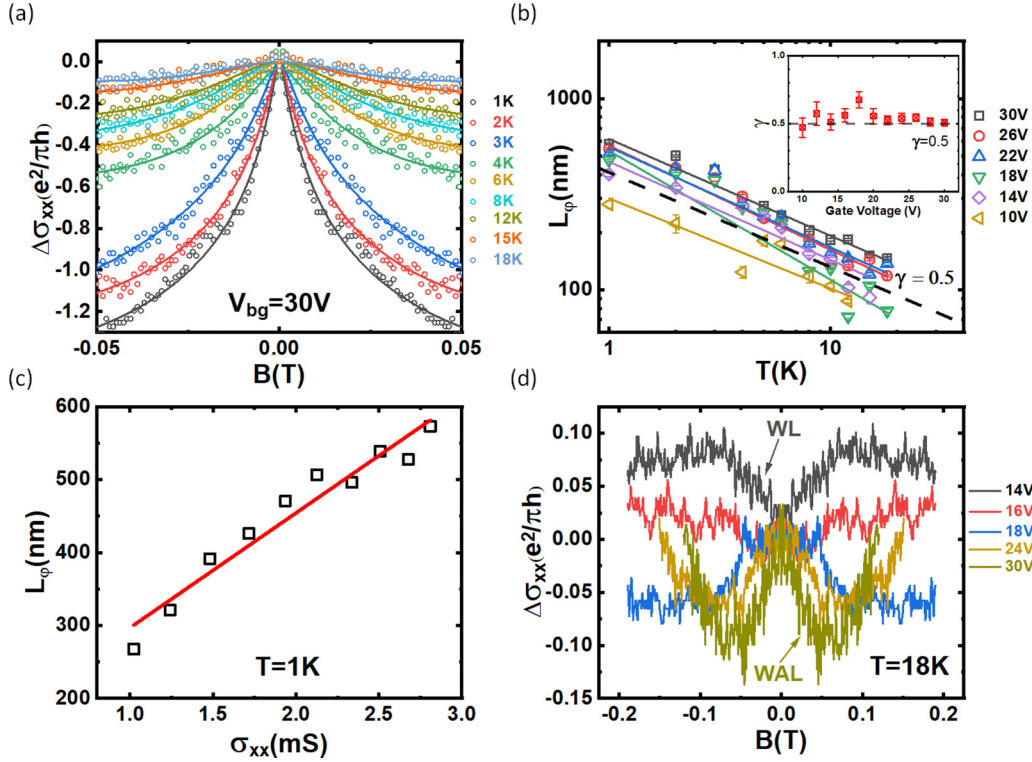


FIG. 5. Temperature dependence of WAL. (a) Theoretical fits (solid lines) with ILP theory to temperature-dependent experimental data (circles) measured at  $V_{bg} = 30$  V. Zero-field conductivity is calculated ( $\sigma_{xx} = 226.6\text{--}227.9 e^2/\pi h$ ). (b) Temperature-dependent phase-coherence length  $L_\phi$  (data points) extracted from WAL at different gate-voltage fits with a power law (solid lines) in a log-log plot (black dashed line is  $\gamma = 0.5$ ). The inset: Gate-dependent coefficient  $\gamma$  extracted from the power-law fitting is close to 0.5 in all gate voltages which indicates the electron-electron interaction is responsible for the dephasing process. (c) Phase-coherence length  $L_\phi$  as a function of the sheet conductance  $\sigma_{xx}$  at  $T = 1$  K. The red line is the linear fitting of  $L_\phi$  and  $\sigma_{xx}$ . (d) Transition from WL to WAL at  $T = 18$  K. Zero-field conductivity is calculated ( $\sigma_{xx} = 104.8\text{--}226.6 e^2/\pi h$ ).

conductance  $\sigma_{xx}$ ). In the meantime, spin-relaxation length  $L_{so}$  decreases with gate voltage [Fig. 3(d)] because of the Rashba and Dresselhaus SOIs. Therefore, WL is observed when the phase-coherence length is  $L_\phi < L_{so}$  at  $V_{bg} = 14$  V. With the increase in gate voltage, WAL emerges under the condition of  $L_\phi > L_{so}$  at  $V_{bg} > 18$  V.

In conclusion, gate-tunable strong spin-orbit interaction-induced WAL has been observed in 2D  $n$ -type Te films. Gate- and temperature-dependent WALs are systematically measured and analyzed. We find that the  $k$ -linear spin-precession vector is much smaller than the  $k$ -cubic spin-precession vector by fitting experimental data with ILP theory. Large phase-coherence length near 600 nm together with gate-tunable SOI make  $n$ -type 2D Te films a competitive candidate for spintronic applications. Furthermore, we determine that the DP spin-relaxation mechanism is dominant and the electron-electron interaction with a small energy

transfer is the main mechanism for inelastic scattering at low temperatures for 2D Te films.

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